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# Spoštovani bralci revije Journal of energy technology (JET)

Proizvodnja električne in toplotne energije iz obnovljivih virov postaja vedno bolj učinkovita in ekonomsko zanimiva. V kombinaciji z okoljevarstvenimi problemi pa postaja izraba obnovljivih virov zelo zaželjena. Ena izmed možnosti izrabe sončne energije je proizvodnja električne energije s pomočjo fotonapetostnih modulov (PV). Druga možnost je s pomočjo solarne termoelektrarne oz. z izrabo tehnologij na osnovi koncentrirane sončne energije (CSP). V ta namen se uporabljajo zrcala, solarni stolp ali pa se zbira toplota v paraboličnih kolektorjih. Toplota pridobljena s pomočjo koncentrirane sončne energije se nato uporablja v Rankinovem procesu za proizvodnjo toplotne in električne energije. V tem trenutku premočno vodijo PV tehnologije. Največ električne energije s pomočjo sonca pridobijo na Kitajskem, na Japonskem, Nemčiji in v ZDA. Energija proizvedena iz sončnih elektrarn pokriva slaba 2 % celotnih svetovnih potreb po električni energiji. Procentualno gledano največ električne energije pridobijo v Hondurasu (približno 12 %) in v Evropi v Grčiji (približno 7 %). Največje fotovoltaične (PV) elektrarne so na Kitajskem, v Indiji in ZDA; in imajo konično moč proizvodnje električne energije že blizu 1 GW. Tudi na področju solarnih termoelektrarn oz. CSP tehnologij se dogajajo zanimivi preboji. Največje solarne termoelektrarne so zgrajene v ZDA; največja ima moč okoli 400 MW električne moči. Razvoj obeh sistemov poteka zelo hitro.

Jurij AVSEC odgovorni urednik revije JET

# Dear Readers of the Journal of Energy Technology (JET)

Production of electricity and heat from renewable sources is becoming more efficient and economically viable. Along with environmental problems it is becoming a necessity utilization of renewable energy sources. One possible use of solar energy is to generate electricity by means of photovoltaic panels technology (PV). Alternatively by means of a solar thermal power plants, or with the use of technologies based on the concentrated solar power technology (CSP). CSP technology uses, the mirrors, the solar tower or collecting heat in the parabolic collectors. The heat produced using solar energy is then used in the Rankine process for the production of heat and electricity. At the moment, the PV technology is dominant. Most electricity by using the sun energy are produced in India, USA and China. Currently sun covers almost 2% of the total electricity consumed in the world. Percentage speaking, most of the electricity generated in Honduras (12%), in Europe, the leading country is Greece (around 7%). The largest photovoltaic power plants are in China, India and the USA. The largest photovoltaic unit Tengger Desert Solar Park in the world have a peak power of electricity production is already over 1 GW. Even in the field of solar thermal power plants respectively. CSP technologies are undergoing interesting breakthroughs, the largest solar thermal power plants are built in the US, the largest lyanpah Solar Power Facility has the power of 392 MW. The development of the PV and CSP systems are under big development.

> Jurij AVSEC Editor-in-chief of JET

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# THE USE OF THE HOOK-JEEVES METHOD FOR THE CALCULATION OF COMPLEX NONLINEAR EQUIVALENT MAGNETIC CIRCUITS

# UPORABA METODE HOOK – JEEVES ZA IZRAČUN KOMPLEKSNIH NELINEARNIH ENAKOVREDNIH MAGNETNIH VEZIJ

Mykhaylo Zagirnyak<sup>33</sup>, Oksana Usatiuk<sup>1</sup>, Volodymyr Usatyuk<sup>1</sup>

**Keywords:** Magnetic system, flow distribution, section method, equivalent circuit, multidimensional parametric optimization, scalarization, criteria-weighted sum method, electromagnetic separator.

# **Abstract**

The Hook-Jeeves method was used as a basis for the development of a magnetic system mathematical model suitable for carrying out engineering and optimization design calculations. It provides minimum expenditure for preparation of initial data, acceptable counting time and automatic convergence at a large interval of input parameter variation. The proposed model also enables highly accurate calculation of nonlinear equation systems describing complex nonlinear magnetic circuits. It is demonstrated that this approach can be used for the creation of design methods for direct current electric devices, in particular, electromagnetic separators.

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### <u>Povzetek</u>

Hook-Jeeves metoda je bila uporabljena kot podlaga pri razvoju matematičnega modela magnetnega sistema, primernega za izvedbo inženirskih izračunov in optimizacije pri načrtovanju. Zagotavlja minimalne izdatke pri pripravi začetnih podatkov, sprejemljivega časa štetja in avtomatsko konvergenco v velikem intervalu variacij vhodnih parametrov. Predlagani model omogoča pridobivanje visoko natančnih izračunov sistemov nelinearnih enačb, ki opisujejo zapletena nelinearna magnetna vezja. Predstavljen pristop je možno uporabiti pri oblikovanju metod za načrtovanje električnih naprav na enosmerni električni tok, zlasti elektromagnetnih ločevalnikov.

# **1** INTRODUCTION

The determination of flux distribution and optimization of magnetic loads in magnetic circuits of various electric devices are carried out on the basis of the calculation of their magnetic systems. The lumped element method is one such calculation method commonly used in engineering, [1]. According to this method, the whole magnetic field is divided into local areas, and the magnetic circuit is divided into a number of sections, and the magnetic circuit device with distributed parameters is substituted by an equivalent complex branched electric circuit with lumped nonlinear parameters. This circuit consists of k nodes, l branches. It is known that, to describe this circuit, (k-1) independent equations can be formulated according to Kirchhoff's first law for the magnetic circuit and (l - k + 1) equations according to Kirchhoff's second law.

However, application of conventional numerical methods (e.g. Seidel's method, Newton's method, etc.), based on relevant iteration processes for the solution of nonlinear equation systems describing electric device equivalent magnetic systems [1], is hampered by a number of challenges. First, the preparation of initial data is laborious: the necessity for the formulation of a Jacobian matrix according to partial derivatives for all the equations in the system; the necessity for assignment of the vector of initial values of the required flux, etc. Second, possible failure of meeting the condition of the iteration process convergence because of the high degree of nonlinearity of the system. Moreover, particular difficulties in the practical realization of these methods are related to the presentation of the solved system as a certain function in a multidimensional space.

### 2 THEORETICAL OUTLINE

The purpose of this paper consists in the creation of a magnetic system mathematical model suitable for carrying out engineering and design calculations. Furthermore, it must guarantee minimum expenditure for the preparation of initial data, acceptable counting time, and automatic convergence at a large interval of input parameters and, at the same time, be sufficiently accurate.

The basis of this mathematical model can be presented by a system of nonlinear algebraic equations written according to Kirchhoff laws. It should describe the equivalent magnetic circuit created by the section method. Such an equation system can be transformed into a mathematical model of multi-criteria parametric optimization, [2].

$$\min_{\vec{x}} \{ f_1(\vec{x}), f_2(\vec{x}), ..., f_k(\vec{x}) \},\$$

where each of the equations in the system will represent a separate objective function  $f_i : \mathbb{R}^n \to \mathbb{R}$ .

In a general case, equations written according to Kirchhoff's first and second laws for the magnetic circuit

$$\sum_{j=1}^{n} \Phi_{j} = 0, \qquad \qquad \sum_{k=1}^{n} U_{k} = \sum_{l=1}^{m} F_{l},$$

cannot be used as objective functions, because it cannot be stated that they are restricted from below and it is possible to find a solution vector that will provide the minimum value  $f(\vec{x}^*)$  of the given function  $f(\vec{x})$  (Fig. 1, solid line).



**Figure 1:** Graphic presentation of magnetic potential closure error in a flux function for a single-loop equivalent circuit (Kirchhoff second law)

To guarantee meeting the requirements to the objective functions within the limits of the solution to the problem of parametric optimization, the equation data are to be presented in the form:

$$f(\vec{x}) = \left| \sum_{j=1}^{n} \Phi_{j} \right|; \qquad f(\vec{x}) = \left| \sum_{k=1}^{n} U_{k} - \sum_{l=1}^{m} F_{l} \right|$$

In this presentation, the equations for Kirchhol first and second laws will be restricted from below by zero at one point (Fig. 1, point A). T point corresponds to the required solution of t initial problem of calculation of flux distributior the magnetic system.

A reworked mathematical model of optimization is formed on the equation syster adequately describing the real magnetic syster and physical processes taking place in it. So, can be stated that the vector of solution to the problem  $\vec{x} = (x_1, x_2, ..., x_n)^T$  will belong to non-empty set  $\vec{x} \in S$ .

Due to the same circumstance, it can also be stated that the vector objective function formed in such a way is convex, and the mathematical model has one global optimum in which the solution vector reflects the only real flux distribution in this magnetic system.

Eventually, the solution to the problem of multi-criteria optimization consists in the search for objective variables (fluxes) vector, meeting the imposed constraints and optimizing the vector function whose elements correspond to the objective functions (the equations of the system).

To lower the degree of optimization of the mathematical model (reduction of the number of objective variables and the number of objective functions), a convolution method, [3], can be used. This method is based on the acceptance of initial values of several fluxes (fluxes-arguments) with the following determination of all the others on the basis of equations of the solved problem. In this case, the same number of equations written by Kirchhoff's second law and included in the system (characteristic equations of the system) remain unused in the process of convolution during the determination of all the fluxes. Thus, it is these initially accepted fluxes-arguments that will be the controlled parameters of optimization, and the characteristic equations will be included into the vector objective function.

As all the objective functions in this problem statement will be of equal weight (the criteria are homogeneous) and mutually "non-conflictive", it is possible to perform scalarization of the vector objective function by the method of weighted sum of criteria (MWSC), [4]

$$F\left(\vec{f}(\vec{x})\right) = k_1 f_1(\vec{x}) + \ldots + k_k f_k(\vec{x}),$$

with all the weight co-efficients equal to one and, thus, to reduce the problem to a one-criterion problem of multidimensional parametric conditional optimization

$$\vec{x}^* \in X: f(\vec{x}^*) = \min_{\vec{x}^* \in X} f(\vec{x}),$$

where

$$X = \left\{ \vec{x} | g_i(\vec{x}) \le 0, i = 1, \dots, m \right\} \subset \mathbb{R}^n.$$

In this case, to reduce the counting time, the acceptable set X can be restricted by zero from below, as the initial equation system takes into account the real directions of the fluxes (negative value corresponds to the opposite direction of the flux) and from above – by the fluxes values calculated for the same equivalent circuit without taking into account the drop of magnetic intensity at nonlinear elements (elements with steel).

The choice of the Hook-Jeeves method, [5], was because it refers to one-criterion methods of multidimensional parametric optimization, requires only calculation of the objective function at approximation points (direct method) and constraints meeting support is easily introduced into its algorithm.

### 3 PROPOSED METHOD AND RESULTS

An equivalent circuit of a roll separator (Fig. 3a) was taken as a calculation equivalent circuit. It is difficult for calculation due to its branched form, and the convergence of five fluxes at node 4 hampers the convolution process. Parameter values (permeances  $\Lambda_i$  and magnetic potential drops  $\Delta U_i$ ) of the magnetic circuit are assumed to be determined by formulas given in [6].

This equivalent circuit (Fig. 3b) is described by the system of equations (Fig. 2).

$$\begin{split} \Phi_{C1} - \Phi_{C2} - \Phi_{S} &= 0 \\ \Phi_{C2} - \Phi_{P2} - \Phi_{PPV} &= 0 \\ \Phi_{P2} - \Phi_{SP} - \Phi_{N2} - \Phi_{D1} - \Phi_{V1} &= 0 \\ \Phi_{D1} + \Phi_{V1} - \Phi_{V3} &= 0 \\ \Phi_{N2} - \Phi_{D2} - \Phi_{N3} - \Phi_{NNV} &= 0 \\ \Phi_{D2} + \Phi_{V3} - \Phi_{V4} &= 0 \\ \Phi_{N3} + \Phi_{D3} - \Phi_{NNT} &= 0 \\ \Phi_{V4} - \Phi_{D3} - \Phi_{V5} &= 0 \\ \frac{F}{2} - \Delta U_{C1} - \Delta U_{C2} - \Delta U_{P1} - \frac{\Phi_{PPV}}{\Lambda_{PPV}} &= 0 \\ \frac{F}{4} - \Delta U_{C1} - \frac{\Phi_{S}}{\Lambda_{S}} &= 0 \\ \frac{F}{4} - \Delta U_{C1} - \frac{\Phi_{S}}{\Lambda_{S}} &= 0 \\ \frac{\Phi_{SP}}{\Lambda_{SP}} - \Delta U_{P2} - \Delta U_{P1} - \Delta U_{C2} - \frac{\Phi_{SP}}{\Lambda_{SP}} &= 0 \\ \frac{\Phi_{V1}}{\Lambda_{SP}} + \Delta U_{N1} + \frac{\Phi_{D1}}{\Lambda_{D1}} - \Delta U_{N2} - \frac{\Phi_{D2}}{\Lambda_{D2}} &= 0 \\ \frac{\Phi_{V1}}{\Lambda_{TV}} + \Delta U_{V1} + \Delta U_{V2} - \frac{\Phi_{D1}}{\Lambda_{D1}} - \Delta U_{N2} &= 0 \\ - \frac{\Phi_{NNV}}{\Lambda_{NNV}} + \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \Delta U_{N3} &= 0 \\ \frac{\Phi_{D2}}{\Lambda_{D2}} - \Delta U_{N3} + \Delta U_{V4} - \frac{\Phi_{D3}}{\Lambda_{D3}} &= 0 \\ \Delta U_{V5} - \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \frac{\Phi_{D3}}{\Lambda_{D3}} &= 0 \\ \end{bmatrix}$$

#### Figure 2: The system of equations

The solution to the above-mentioned equation system concerning 17 unknown parameters is rather difficult. Therefore, to decrease the number of the independent equations, the convolution is used:

1) Flux  $\Phi_{{\it C}1}$  is used as the first flux-argument.

- 2) Circuit II. Flux  $\Phi_{\scriptscriptstyle S}=\Lambda_{\scriptscriptstyle S}\cdot(\frac{F}{4}-\Delta U_{\scriptscriptstyle C1})$  is determined.
- 3) Node 2. Flux  $\Phi_{C2} = \Phi_{C1} \Phi_S$  is found.

- 4) Circuit I. Flux  $\Phi_{PPV} = \Lambda_{PPV} \cdot (\frac{F}{2} \Delta U_{C1} \Delta U_{C2} \Delta U_{P1})$  is determined.
- 5) Node 3. Flux  $\Phi_{\scriptscriptstyle P2} = \Phi_{\scriptscriptstyle C2} \Phi_{\scriptscriptstyle PPV}$  is found.

6) Circuit III. Flux  $\Phi_{SP} = \Lambda_{SP} \cdot \left(\frac{F}{4} + \frac{\Phi_S}{\Lambda_S} - \Delta U_{P2} - \Delta U_{P1} - \Delta U_{C2}\right)$  is determined.



a)





b)

Thus, fluxes  $\Phi_{P2}$  and  $\Phi_{SP}$  are determined via the known value of flux-argument  $\Phi_{C1}$  by convolution of the equivalent circuit. To solve the equation for node 4 we have to assign two more fluxes-arguments, for which purpose we choose fluxes  $\Phi_{V1}$  and  $\Phi_{D1}$ .

- 7) Node 4. Flux  $\Phi_{N2} = \Phi_{P2} \Phi_{SP} \Phi_{V1} \Phi_{D1}$  is found.
- 8) Node 5. Flux  $\Phi_{V3} = \Phi_{D1} + \Phi_{V1}$  is determined
- 9) Circuit V. Flux  $\Phi_{D2} = \Lambda_{D2} \cdot (\Delta U_{V3} + \Delta U_{N1} + \frac{\Phi_{D1}}{\Lambda_{D1}} \Delta U_{N2})$  is determined
- 10) Circuit IV. Flux  $\Phi_{_{NNV}} = \Lambda_{_{NNV}} \cdot (\frac{\Phi_{_{SP}}}{\Lambda_{_{SP}}} \Delta U_{_{N2}})$  is found
- 11) Node 7. Flux  $\Phi_{V4} = \Phi_{V3} + \Phi_{D2}$  is found.
- 12) Node 6. Flux  $\Phi_{\scriptscriptstyle N3}=\Phi_{\scriptscriptstyle N2}-\Phi_{\scriptscriptstyle D2}-\Phi_{\scriptscriptstyle NNV}$  is found.
- 13) Circuit VIII. Flux  $\Phi_{D3} = \Lambda_{D3} \cdot (\frac{\Phi_{D2}}{\Lambda_{D2}} \Delta U_{N3} + \Delta U_{V4})$  is determined.
- 14) Node 9. Flux  $\Phi_{V5} = \Phi_{V4} + \Phi_{D3}$  is found.
- 15) Node 8. Flux  $\Phi_{\scriptscriptstyle NNT} = \Phi_{\scriptscriptstyle N3} \Phi_{\scriptscriptstyle D3}$  is found.

Thus, we managed to determine the remaining 14 fluxes when the values of three fluxesarguments  $\Phi_{CI}$ ,  $\Phi_{VI}$   $\mu \Phi_{DI}$  were assumed. Now, the correctness of the assumed initial values of fluxes is to be determined using Kirchhoff's second law for independent closed circuits (that did not take part in convolution). In this case, these are circuits VI, VII and IX (Fig. 3). The characteristic equations of the system are of the form:

$$f_1(\vec{x}) = \left| \frac{\Phi_{V1}}{\Lambda_{TV}} + \Delta U_{V1} + \Delta U_{V2} - \frac{\Phi_{D1}}{\Lambda_{D1}} - \Delta U_{N2} \right|;$$
$$f_2(\vec{x}) = \left| -\frac{\Phi_{NNV}}{\Lambda_{NNV}} + \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \Delta U_{N3} \right|;$$
$$f_3(\vec{x}) = \left| \Delta U_{V5} - \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \frac{\Phi_{D3}}{\Lambda_{D3}} \right|.$$

The scalar form of the objective function will be obtained on the basis of these characteristic equations:

$$F\left(\vec{f}\left(\vec{x}\right)\right) = \begin{vmatrix} \left(\frac{\Phi_{V1}}{\Lambda_{TV}} + \Delta U_{V1} + \Delta U_{V2} - \frac{\Phi_{D1}}{\Lambda_{D1}} - \Delta U_{N2} \right) + \\ + \left(-\frac{\Phi_{NNV}}{\Lambda_{NNV}} + \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \Delta U_{N3} \right) + \left(\Delta U_{V5} - \frac{\Phi_{NNT}}{\Lambda_{NNT}} + \frac{\Phi_{D3}}{\Lambda_{D3}} \right), \end{cases}$$

which can be minimized by the Hook-Jeeves method in a 3D space of input-controlled parameters ( $\Phi_{C1}$ ,  $\Phi_{V1}$  and  $\Phi_{D1}$ ).

The calculation results were analogous to those of [7], and the attained accuracy exceeds the accuracies presented in Table 2, [7] for corresponding nodes and circuits.

# 4 CONCLUSIONS

The obtained results and positive experience make it possible to recommend the application of this approach to the solution of nonlinear equation systems describing complex, branched magnetic equivalent circuits. In turn, the absence of difficulties with the convergence of iteration process of searching solutions to many fluxes-arguments also provides the possibility to abandon simplification of the topology of equivalent circuits and to completely take into consideration the real pattern of flux distribution. Hereafter, the authors will to verify the tempo of the solution of such optimization problems by other methods of multidimensional optimization and use this method in the generation of engineering methods for designing direct current electric devices, in particular, electromagnetic separators.

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# ANALYTICAL ESTIMATION OF SWITCHED RELUCTANCE MOTOR FLUX LINKAGE PROFILE BY USING EVOLUTIONARY ALGORITHM AND NUMERICAL SIMULATIONS

# ANALITIČNA OCENA MAGNETNIH SKLEPOV PREKLOPNO RELUKTANČNEGA MOTORJA Z UPORABO EVOLUCIJSKEGA ALGORITMA IN NUMERIČNIH SIMULACIJ

Marinko Barukčić<sup>138</sup>, Željko Hederić<sup>1</sup>, Tin Benšić<sup>1</sup>

**Keywords:** estimation, evolutionary algorithm, flux linkage profile, numerical simulation, switched reluctance motor

# **Abstract**

The objective of this paper is to research the possibility of approximating a switched reluctant motor (SRM) flux linkage with respect to rotor angle and current with an analytical expression. The flux linkage per phase of the reluctance motor stator winding is obtained numerically for different rotor positions. The numeric values of the stator flux linkage are calculated with Finite Element Method (FEM) software FEMM (Finite Element Method Magnetics). After the flux linkage values are obtained the function estimate is proposed. This function represents the change in the stator flux linkage with respect to rotor angle. The form of proposed function is based on the curve shape obtained from FEMM. The proposed analytical expression contains some parameters with unknown values that need to be determined.

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The Evolutionary Algorithm (EA) is used for this purpose. The problem of finding function parameters is defined in the form of the optimization problem, which is solved by EA. The problem objective function is defined as the difference between the flux linkage values obtained by using FEMM and calculated by using the proposed analytical expression. The above procedure is performed for a few specified current values. The flux linkage values for any current values are obtained by linearization between specified current values. The proposed analytical model of the motor flux linkage can be implemented in simulation model of the SRM with the aim of controlling it. Furthermore, the SRM inductance profile can be easily obtained by dividing the proposed flux model by current.

### <u>Povzetek</u>

Namen članka je raziskati možnosti ocenjevanja magnetnih sklepov preklopno reluktančnega motorja (PRM) v povezavi s kotom zasuka rotorja in tokom. Vrednosti magnetnih sklepov posamezne faze statorskega navitja preklopno reluktančnega motorja se pridobijo z numeričnimi izračuni pri različnih kotih zasuka rotorja. Uporabljena je metoda končnih elementov (MKE) z uporabo programske opreme FEMM (Finite Element Method Magnetics). Po končanem izračunu magnetnih sklepov je predlagana cenilna funkcija, ki predstavlja spremembo magnetnih sklepov statorja glede na kot zasuka rotorja. Oblika predlagane funkcije temelji na obliki krivulje pridobljene s pomočjo FEMM. Predlagan analitični izraz vsebuje določene parametre z neznanimi vrednostmi, ki jih je potrebno določiti z evolucijskim algoritmom (EA). Rešitev iskanja funkcijskih parametrov je opredeljena v obliki optimizacijskega problema, ki se rešuje s pomočjo EA. Predlagana funkcija je opredeljena kot razlika vrednosti magnetnih sklepov, pridobljenih s pomočjo FEMM, in izračunanih s pomočjo predlaganega analitičnega izraza. Postopek je izveden pri določenih vrednostih tokov. Vrednosti magnetnih sklepov ostalih tokov pa so pridobljene z linearizacijo med določenimi vrednostmi tokov. Predlagan analitični model magnetnih sklepov preklopno reluktančnega motorja je mogoče uporabiti pri vodenju simulacijskega modela PRM.

### 1 INTRODUCTION

Research of the switched reluctance motor inductance/flux linkage dependence on rotor angle is a topic of interest for many researchers. This dependence is important for mathematical modelling, calculation and simulation of SRM with the purpose of SRM controlling. As it is mentioned in [1] and [2] finding the inductance/flux linkage is one of the crucial parameters for reluctance motor performance calculation. There are different approaches in calculating and modelling inductance dependence on rotor angles. In [3], an analytical approach for the calculation of switched reluctance motor inductance in unaligned positions is presented. Analytical method for aligned and unaligned flux linkage of the switched reluctance motor is also presented in [1], [4], [5], and [6]. Calculation of inductance profile of the linear switched reluctance motor by using an analytical approach is given in [7]. In [8], the hybrid method based on soft computing techniques Artificial Neural Networks (ANN) and Fuzzy Inference System (FIS) are used to estimate inductance of the motor. In [1], the measured data is used for validation of expressions used for inductance estimation. The numerical calculation methods (for example Finite Element Method (FEM)) have been used for analytical model validations in recent times. The FEM method is used in [9] for validation of the measurement method for reluctance motor

inductance. In [10], the FEM method is also used for the performance analysis of switched reluctance motors.

The hypothesis according to the research performed in the paper assumes that it is possible to find analytical expressions for the motor flux linkage based on numerical discrete flux linkage values obtained by measurement or simulation. The proposed approach uses only numerical values of the measured (simulated) flux linkage unlike analytical approaches in literature that use motor construction (geometry) data. The idea is to propose an analytical function with similar shapes of the numerical flux linkage value forms. According to the above, the problem is to solve parameter values identification of the function so its curve fits as close as possible to numerical flux linkage values. For the best presentation of the performed research, the paper structure is organized in three main parts: defining the optimization problem, a short overview of used EA method, and a simulation example.

# 2 OPTIMIZATION PROBLEM DEFINITION AND SOLVING

#### 2.1 Basic Idea

Fig. 1 and 2 show examples of reluctance motor flux linkage changes with respect to rotor angle and current in a range from unaligned to aligned rotor positions. The function graph in Fig. 1 is sigmoid-shaped with respect to rotor position. Because of that, the Gompertz function is proposed for flux linkage estimation. The Gompertz function is chosen from among other sigmoid functions because it is easy to change the shape of the function by changing its parameter values.



Figure 1: An example of flux linkage in as a function of rotor angle and current

The linear combination of three Gompertz functions used for estimation of motor flux linkage is:

$$G_{1}(\theta) = p_{1} \cdot exp\left(-exp\left(p_{2} \cdot (p_{3} - \theta)\right)\right)$$
(2.1)

$$G_{2}(\theta) = p_{4} \cdot exp\left(-exp\left(p_{5} \cdot (p_{6} - \theta)\right)\right)$$
(2.2)

$$G_3(\theta) = p_7 \cdot exp\left(-exp\left(-p_8 \cdot (p_9 - \theta)\right)\right) - p_7$$
(2.3)

$$\Psi_{C}(\theta, I) = \sum_{i=1}^{3} G_{i}(\theta) + p_{10} \cdot I$$
(2.4)

where  $\theta$  is rotor angle in rad,  $p_1$ ,  $p_4$ ,  $p_7$  are function parameters that define function asymptotes in Wb;  $p_2$ ,  $p_5$ ,  $p_8$  are function parameters that define function slopes in 1/rad;  $p_3$ ,  $p_6$ ,  $p_9$  are function parameters that define graph translations along horizontal axis in rad,  $p_{10}$  is a constant value parameter in Wb/A and *I* is current value for which analytical expression (2.4) is valid. Parameters  $p_1 - p_{10}$  are positive numbers.



Figure 2: An example of flux linkage as a function of rotor angle and current

#### 2.2 Optimization problem formulation

The optimization problem represents the minimization of differences between measured or simulated by FEMM flux linkage values ( $\Psi_S$ ) and calculated values ( $\Psi_C$ ) according to (2.4) for the i-th rotor position (angle). Thus, the optimization problem objective function is defined in form of the square sum of differences between measured and calculated inductance values relative to the measured values for *N* rotor positions:

$$OF(p_{1}, p_{2}, p_{3}, p_{4}, p_{5}, p_{6}, p_{7}, p_{8}, p_{9}, p_{10}, \theta, I) =$$

$$100 \cdot \sum_{i=1}^{N} \left[ \left( \Psi_{C,i}(\theta_{i}, I) - \Psi_{S,i}(\theta_{i}, I) \right)^{2} / \Psi_{S,i}(\theta_{i}, I) \right] \rightarrow min$$
subject to:  $p_{1} > 0, p_{2} > 0, p_{3} > 0, p_{4} > 0, p_{5} > 0,$ 

$$p_{6} > 0, p_{7} > 0, p_{8} > 0, p_{9} > 0, p_{10} > 0.$$
(2.5)

Parameters  $p_1 - p_{10}$  are problem decision (problem output) variables that need to be found by an optimization method. Known *N* flux linkage values  $\Psi_S$  and rotor positions  $\theta$  are problem input variables.

#### 2.3 Optimization method

The optimization problem defined in (2.5) is nonlinear due to (2.1)-(2.4). It can be solved with different metaheuristic population based methods, *[11]*. A Genetic Algorithm (GA) that belongs to a class of Evolutionary Algorithms (EAs) is used in the paper to solve the optimization problem (2.5). The main structure of the GA (EA) is given in Fig. 3. The possible solution of problem (2.5) is represented by individuals in GA (EA). For problem (2.1)–(2.4) GA individual (individual chromosome) consists of ten genes. The representation of the GA individual in vector form and GA population (set of individuals) in matrix form can be seen in Fig. 4. Because GA (EA) are very well described in literature, the details about GA are not given here. The GA details can be seen in literature e.g. in *[12]*.



Figure 3: Basic structure of GA

#### 2.4 Estimation of flux linkage at any current values

After problem (2.5) is solved, the analytical expressions of flux linkage at specified current values are obtained according to (2.4). The linearization procedure is applied to obtain flux linkage values at any current between the specified current values (Fig. 5). The specified current values used for solving problem (2.5) are determined based on the flux linkage profile for the aligned rotor position (Fig. 5). The linearization is performed according to:

$$\Psi(\theta, I) = \Psi(\theta, I_j) + \frac{\Psi(\theta, I_{j+1}) - \Psi(\theta, I_j)}{I_{j+1} - I_j} \cdot (I - I_j)$$
(2.6)

# 3 AN EXAMPLE OF PROPOSED METHOD USAGE

The method proposed in Section 2 is tested on an example of a 6/4 switched reluctance motor. The method described in Section II. is performed using the following steps:

- Step 1.: Simulation of switched reluctance motor is performed in FEMM software, [13], and numerical flux linkage values with respect to rotor angle at specified current values are obtained.
- Step 2.: Optimization problem (2.5) is solved with GA and values for parameters p<sub>1</sub> p<sub>10</sub> are obtained for each specified current value.
- Step 3.: Analytical expressions for motor flux linkage estimation are determined according to (2.4) with the use of parameter values obtained in Step 2, and then they are used to estimate flux linkage at any current and rotor angle values according to (2.6).

#### 3.1 Data of reluctance motor and GA parameters

The example of motor geometry used to test the method is shown in Fig. 6. The motors physical dimensions are modelled similar to those presented in *[10]*. The reluctance motor has six poles on the stator and four poles on the rotor. For such a geometry, the rotor angle for the aligned rotor position is 45° considering that the angle for the unaligned rotor position is 0°. The motor geometry and materials data are given in Table 1.

GA parameters and genetic operators used for optimization: initial population randomly generated, population size of 5000 individuals, number of generations 250, number of elite individuals 2, tournament type of selection operator, and scattered type of crossover operator.

$$IND_{i} = \begin{bmatrix} p_{1i} & p_{2i} & p_{3i} & p_{4i} & p_{5i} & p_{6i} & p_{7i} & p_{8i} & p_{9i} & p_{10i} \end{bmatrix}$$
$$POP = \begin{bmatrix} IND_{1} \\ \vdots \\ IND_{M} \end{bmatrix}$$

Figure 4: Individual (IND) and population (POP) in GA.

#### 3.2 Simulation results

Table 2 specifies the current values used in FEMM simulations, and linearization ranges are presented. The FEMM simulations are performed for 90 rotor positions in rotor angle steps of 0.5° in range from 0° (unaligned position) to 45° (aligned position).

After FEMM simulations are complete, the optimization of the problem (2.5) is performed by using GA. The parameter  $p_1$ - $p_{10}$  solutions are obtained and shown in Table 3 for each specified current value.



*Figure 5:* Determination of specified current values for flux linkage linearization with respect to current



Figure 6: Reluctance motor with six poles on stator and four rotor poles

<b>TUDIE 1.</b> WOLDI GEOMELIY UUL	Table	1: Moto	r geometry	data
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Air gap	0.24 mm
Dro (rotor outer diameter)	37.84 mm
Dri (rotor inner diameter)	22.10 mm
Dj (stator yoke thickness)	6.5 mm
Stack Length	50 mm
Magnetomotive force	80 Ampere turns
Material	M-15 Steel from FEMM
	materials library

Table 2: Specified current values used in FEMM simulations

j	1	2	3	4	5
/ <sub>j</sub> (A)	0.01	0.05	0.1	0.5	1
I <sub>j+1</sub> (A)	0.05	0.1	0.5	1	1.5
j	6	7	8	9	10
/ <sub>j</sub> (A)	1.5	2	2.5	3	4
I <sub>j+1</sub> (A)	2	2.5	3	4	8
j	11	12	13		
/j (A)	8	12	20		

In Fig. 7, FEMM is simulated ( $\Psi_S$ ) and according to (2.4) and (2.6) estimated ( $\Psi_C$ ) flux linkages for specified current values are presented. In Fig. 8, a detailed overview of some results from Fig. 7 is given. As can be seen from Fig. 7 and 8, the analytical representation of flux (2.4) for specified current values fits the reluctance motor flux linkages obtained by FEM simulation very well. Accordingly, it can be concluded that flux linkage of switched reluctance motor as function of rotor angle obtained by using numerical simulations can be analytically estimated by the presented method (2.4) with high accuracy.

After obtaining the analytical model of flux linkage with respect to rotor position for all specified current values, the estimation of flux linkage at any rotor angle and stator current values can be obtained by linearization with respect to current. The simulation results for current values different from specified current values in Table 2 are presented in Fig. 9. The detailed results for some of the current values from Fig. 9 are presented in Fig. 10. Again, the analytical calculated flux linkage according to (2.6) has good accuracy, as can be seen from Fig. 9 and 10. The highest error among the simulated current values in Fig. 9 was for the current of 6 A as can be seen in Fig. 10. This error can be decreased by narrowing the current range for linearization.

j	<i>p</i> <sub>1</sub>	<i>p</i> <sub>2</sub>	<i>p</i> <sub>3</sub>	<i>p</i> <sub>4</sub>	<b>p</b> 5
1	2.07E- 04	8.10	0.3471	1.38E- 04	7.48
2	0.0011	7.72	0.3674	5.36E-	8.60
3	0.0023	7.43	0.3626	0.0011	8.43
4	0.0121	7.48	0.3727	0.0065	8.86
5	0.0233	7.55	0.3546	0.0142	7.98
6	0.0325	8.25	0.3571	0.0252	7.83
7	0.0476	7.54	0.3685	0.0249	8.82
8	0.0620	7.56	0.3731	0.0359	7.09
9	0.0735	7.35	0.3616	0.0375	8.38
10	0.0866	7.71	0.3651	0.0436	7.07
11	0.1014	6.99	0.3499	0.0446	6.74
12	0.0972	6.27	0.3398	0.0564	4.17
13	0.0942	6.16	0.3157	0.0348	3.38
j	<b>p</b> <sub>6</sub>	<b>p</b> 7	<b>p</b> <sub>8</sub>	<b>p</b> 9	<b>p</b> <sub>10</sub>
1	0.6379	4.41E-	99.87	0.2172	0.0032
2	0.6482	2.21E-	54.72	0.4222	0.0032
3	0.6518	4.28E-	87.70	0.2116	0.0032
4	0.6401	6.34E-	16.20	0.5765	0.0032
5	0.6417	7.50E-	62.06	0.2165	0.0032
6	0.6422	0.0010	39.66	0.6122	0.0032
7	0.6277	9.84E-	76.67	0.5449	0.0032
8	0.6647	0.0018	31.88	0.4470	0.0032
9	0.6495	0.0020	71.28	0.2140	0.0032
10	0.5865	0.0046	32.40	0.4592	0.0032
11	0.5871	0.0073	34.47	0.7502	0.0031
12	0.5712	0.0075	37.61	0.7521	0.0031
13	0.5106	0.0069	19.39	0.7223	0.0031

**Table 3:** Solution of optimization problem (2.5) for specified current values in Table 2

Analytical estimation of switched reluctance motor flux linkage profile by using evolutionary algorithm and numerical simulations



Figure 7: Flux linkage simulation results for specified current values (Table 2)





**Figure 8:** Flux linkage simulation results for some of specified current values (0.01 A, 4 A and 20 A)

Analytical estimation of switched reluctance motor flux linkage profile by using evolutionary algorithm and numerical simulations



*Figure 9:* Flux linkage simulation results for current values different from specified current given in Table 2





**Figure 10:** Flux linkage simulation results for some of current values in Fig. 9 (0.05 A, 6 A and 10 A)

# 4 CONCLUSION

The research on switched reluctance motor flux linkage profile estimation with respect to rotor angle and current using the analytical expression is presented in this paper. The proposed analytical expression is a linear combination of three Gompertz functions and constant value. The optimization problem needs to be solved in order to obtain parameters for proposed flux linkage expression. The objective function of the problem is the difference between measured or numerically simulated and analytically calculated inductance values. Due to its complexity, the optimization problem is solved with GA.

It is shown in this paper that switched reluctance motor flux linkage with respect to rotor angle and current can be successfully estimated with the proposed analytical expression and linearization with respect to current. The advantage of the proposed method is the high accuracy of estimated flux linkage profile with respect to rotor position. The drawback of the proposed method is the high number of model parameters that need to be determined.

Further research will be focused on implementation of the proposed method in simulation software (in form of block) for the simulation of switched reluctant motor controlling.

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#### Nomenclature

G <sub>1,2,3</sub> (θ)	Gompertz function with respect to rotor angle
θ	rotor angle
<b>p</b> 1-9	Gompertz function parameters
<b>p</b> 10	constant value parameter
₩с	flux linkage values obtained by FEMM simulations
Ψs	flux linkage values calculated according to proposed model
1	stator current value
OF	objective function value
N	number of rotor positions
<b>I</b> j	Specified current values
¥( <i>θ,</i> I)	flux linkage profile with respect to a rotor angle $ heta$ and a current I
Dj	stator yoke thickness
Dri	rotor inner diameter
Dro	rotor outer diameter



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# EFFICIENT APPLICATIONS AND ARCHITECTURE OF MODERN DIGITAL SIGNAL PROCESSORS

# UČINKOVITE APLIKACIJE IN ARHITEKTURE MODERNIH DIGITALNIH SIGNALNIH PROCESORJEV

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**Keywords:** digital signal processor, parallel processing, Harvard processor architecture, evaluation model

# Abstract

Digital signal processors have found their roles in various fields of science and technology. With the appearance of problems related to the processing of large quantities of data in real time, it was necessary to develop a system that would execute procedures very rapidly and at low cost. The most common application in real time is the digitization and mathematical processing of audio, video, temperature, and voltage data, etc., resolved using parallel operations. Various producers of digital signal processors have developed processors and evaluation models that enable developers to quickly and efficiently create unique applications in communications and visual systems, biomedicine, meteorology, etc. In this article, the basic performance and architecture of the modern digital signal processor are described in detail with emphasis on the most common applications. A practical example of the use of a digital signal processor for numerical integration is presented. A comparison with commonly used processors is performed to confirm its efficiency.

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### Povzetek

Digitalni signalni procesorji se pojavljajo v različnih panogah znanosti in tehnologije. S pojavom problemov, ki zahtevajo procesiranje velikih količin podatkov v realnem času, je bilo potrebno razviti sistem, ki je sposoben izvajati operacije z večjo hitrostjo in nižjimi stroški. Najpogostejše aplikacije v realnem času so digitalizacija, matematično procesiranje avdio in video signala, temperature, napetosti ipd., ki se izvajajo z vzporednimi operacijami. Različni proizvajalci digitalnih signalnih procesorjev so razvili procesorje in ocenjevalne postopke, ki omogočajo razvijalcem hitro in učinkovito ustvarjanje edinstvenih aplikacij na področju telekomunikacij, vizualnih sistemov, biomedicine, meteorologije ipd. V članku je podrobno opisano osnovno delovanje in arhitektura modernih digitalnih signalnih procesorjev s poudarkom na najpogosteje uporabljenih aplikacijah. Predstavljen je praktični primer aplikacije digitalnega signalnega procesorja za numerično integracijo. Za potrditev učinkovitosti je podana primerjava z drugimi pogosto uporabljenimi tipi procesorjev.

# 1 INTRODUCTION

Digital signal processors (DSP) are used for collecting large amounts of data, which are the subject of mathematical transformations that give very good results in real time systems. Due to their basic characteristics, DSP application vary from practical everyday devices (cell phone, camera, etc.) to medical, military, scientific research and evolutionary models.

The first appearance of the DSP was in the 1970s, and it was first dominant in telecommunications, high-speed modems, military applications and medicine, because these fields could financially support the development of the expensive technology at that time. A group of engineers from Texas Instruments (TI) presented the first commercial DSP whose architecture is the closest to today's DSPs at International Solid-State Circuits Conference (ISSCC) in February 1982. Their first device was the TMS32010 with 5 million instructions per second and with 55,000 transistors, [1]. To enter the consumer market, they created a talking and listening doll named Julie, and the TMS320C17 was used for voice recognition. They also wanted to attract more customers and expand into more areas, so they started from the basic knowledge of digital signal processing and observed huge losses of energy; their aim was to reduce it, [1]. Nowadays, most of the devices that process graphics and sounds cannot be imagined without a specialized DSP processor.

In this paper, the authors analyse the basic features and architecture of DSPs. The paper is structured as follows: Section 2 presents basic performance and the architecture of DSPs; Section 4 presents the most commonly used applications and algorithms using DSPs; practical implementation is presented on a Texas Instrument evaluation model in Section 4.

### 2 BASIC PERFORMANCE AND ARCHITECTURE OF THE DSP

A DSP is a microprocessor that has high data flow and can process fast streaming, e.g. multimedia data processing. The execution time of the program using a DSP can be predicted and thus desirable results are guaranteed. It is possible to obtain different behaviour from the system through the reprogramming of the DSP with relevant software, i.e. with decoding algorithm execution, [2]. Programs written for regular processors are written in high-level
programming languages, but programs for the DSP are more commonly written in an assembly language because of the standard DSP architecture (multiple memory spaces, buses, irregular sets of instructions and highly specialized hardware), [3]. A DSP is a microprocessor designed for fast problem solving in digital signal processing, in particular for the rapid execution of arithmetic and logical operations and has the capability of executing one or more parallel multiply-accumulate (MAC) operations in one instruction cycle. The time of the MAC operations execution is not a primary feature of the DSP, but faster MAC operations provide better bandwidth. Due to the latter, two or more MAC units are embedded in modern DSPs. MAC operations are common in DSP applications, and they are used for vector multiplication, digital filters, correlations and Fourier transformations, [4], [5]. DSPs are commonly used for real-time processes, and they receive real time signals for audio, video, temperature, pressure or location that have to be digitized and mathematically processed in real time. They are designed for fast execution of the finite impulse response filters (FIR), which are used in digital signal processing. A FIR filter is implemented in real-time and uses circular buffering carried out through the steps listed below. The 14 steps are running parallel on a DSP, unlike on a traditional microprocessor where they are serially executed [4], [5]. Because the algorithm has to be executed quickly, internal DSPs architecture allows the execution in one cycle operations of the loop which contains steps 6-12 and they are repeated circularly, [5].

Selecting an adequate digital signal processor is an important but not easy task due to the great number of available processors. It is necessary to consider the following, [6]:

• architectural features – when selecting a DSP, it is important to pay attention to onchip memory, input/output options, RAM etc. because DSPs are not multifunctional

• execution speed – even though there are two basic measurement units of the CPU clock speed (MHz) and the number of instructions processed per second that a computer can process (MIPS), due to the various numbers of multiple operations of different DSPs, an alternative measure is based on a speed performance benchmark algorithm.

• type of the arithmetic – although most of the PDSPs use fixed-point arithmetic, floating point arithmetic is more efficient, more precise and needs less execution time but, because of optimized DSP arithmetic, the speed is approximately equal. For temporarily storing the results of DSP with fixed-point arithmetic, the additional accumulator registers are joined.

• word length – DSP with fixed-point designed for telecommunications uses 16-bit word length and processors intended for high-quality 24-bit word length audio applications. DSP with floating point arithmetic uses the 32-bit word length.

In standard microprocessors, based on Von Neumann architecture, operations are executed sequentially, which commonly results in data flow congestion, as shown in Fig. 1. When aspiring for a faster processor and faster execution of the mathematical instructions in digital signal processing, it is necessary to separate the buses, i.e. use dual bus architecture (separate memory for data and memory for program instructions). This concept of processor is called Harvard architecture, and it is used in most of the modern DSPs; it is presented in Fig. 1, [5]–[7]. The use of two separate memory buses assures simultaneous data and instruction flow and provides the ability for fetching more options in every instruction cycle, [8].



Figure. 1. Von Neumann processor architecture



Figure 1: Harvard processor architecture

The DSP processor consumes most of the loop execution time in the algorithms, so it has a builtin CPU instruction cache that can store the 32 most commonly used programming instructions. This processor concept is called Super Harvard Architecture (SCHARC) (presented in Fig. 2) designed by engineers of the Analog Devices company, which unified the enhanced DSP under the name SHARC®DSP. To accelerate the information flow, they have connected it to the data memory I/O controller, which provides high-speed parallel and serial communications ports, [5].



Figure 2: Super Harvard processor architecture

A specific feature of the Harvard architecture is the instruction overlap, i.e. instruction pipelining which allows the CPU to execute all execution steps (fetch, decode, execute) in parallel, [6]. The ability for instruction pipelining (presented in Fig. 3) is a significant element for achieving high processor performances in digital signal processing, [2].



TIME (in clock cycles)

#### Figure 3: Instruction pipelining

The number of levels of parallel instruction execution differs from processor to processor: as the number of levels is higher, the performances of the processor are better, i.e. studying the parallel instruction execution leads to reduced average execution time of the instructions. Aiming to enhance the memory and speed memory access in one instruction cycle, various producers have modified the Harvard processor architecture in different ways, [2].

For DSP performance improvement, two approaches of parallel processing were developed: VLIW (Very Long Instruction Word) and SIMD (Single-Input Multiple-Data). The VLIW processor architecture is suitable for numerically demanding algorithms due to embedded multiple units for the parallel execution of instructions in one cycle. More details about parallel processing can be found in [2], [9], [10]. The SIMD processor architecture is used in operations of big data groups, e.g. matrix operations, image processing, graphics, simulations, numerical analysis, etc., [2].

## 3 MOST COMMONLY USED APPLICATIONS AND ALGORITHMS

It is important to consider the requirements of the applications that would be executed on the desired DSP. Dominant producers in sales and the development of the DSPs are presented in Table 1 with a list of applications and algorithms from literature:

Producers	DSPs	APPLICATIONS AND ALGORITHMS
Analog Devices	ADSP-21xx 16bit, fixed point; 32bit, floating and fixed point	wideband sinusoidal (WS) speech, [11], Dual Tone Multi-Frequency (DTMF) signals, [12]; image processing and resilient propagation algorithms, [13]; intravascular ultrasound, [14], active power filter, [15]; image reconstruction algorithms, [16]
	Blackfin	Optimization of MP3 decoder, [17]; audio equalizer, [18], driver fatigue detection system, [19], [20]; fuzzy logic controller, [21], guitar effectors [22], H.264/AVC encoder, [23], graphic equalizer, [24]
Lucent Technologies and AT&T	DSP16xx 16bit, fixed point; DSP32xx 32bit, floating point	multineuron recordings, [25] multi-channel dual-tone multiple frequency detection, [26]; digital lock in amplifier, [27]; matrix-pencil approach, [28]; noise cancellation, [29]; control of brushless DC (BLDC) drives, [30]
Motorola	DSP561xx 16 bit, fixed point; DSP560xx 24 bit, fixed point; DSP653xx 24 bit, fixed point; DSP96002 32 bit, floating point	Extracting signal components, [31]; real-time speech compression, [32]
	StarCore	Radix-4 FFT, [33]; least mean square adaptive filter algorithm, [34]; convolutional face finder algorithm (for teleconferencing, security access control, etc.), [35]
Texas Instruments	TMS320Cxx 16 bit, fixed point; TMS320Cxx 32 bit, floating point	rapid prototyping, [36]; acoustic OFDM transmitter, [37]; voltage frequency control of induction motor drive, [38]; LISA models, [39]; active noise control, [40]; noise reduction in speech signals, [41]
	TMS320LF	temperature humidity detection, [42]

Table 1: An overview	of DSP	annlications	and alaorithms
TUDIC I. AN OVERVIEW	0 0 0 0 0 0 0	applications	una argontinns

DSP is present in all areas where the information is processed in digital form or controlled using digital processors, some of which are shown in Table 2, [5], [43].

AREA	DSP algorithm	APPLICATION
Communication	Speech coding/decoding; speech encryption/decryption; speech recognition; speech synthesis; speaker identification; echo cancellation; data compression;	Digital mobile telephony, [44]; multimedia computers, secure communications; satellite phones; robotics; automotive applications; multimedia workstations; speakerphones; modems;
	Modem algorithms	Digital mobile telephony; digital audio broadcast; digital television
Consumer	Noise cancellation; audio equalization; ambient acoustics emulation; audio mixing and editing; sound synthesis	Consumer/professional audio; music; multimedia computers, [45]; advanced user interfaces
	Vision; image compression/decompression; image compositing	Robotics; security; multimedia computers; navigation; digital video [46]; digital photography; consumer video; advanced user interfaces;
Industrial, medicine and military	Image processing, beamforming	Magnetic resonance imaging (MRI)[47]; ultrasound, [48]; CT; ECG, [49]; process monitoring and control, [50], [51]; vision systems, [52]; navigation; radar/sonar, [53]; digital radio;

### Table 2: DSP fields of use and applications

Communication systems and audio application

o Adaptive echo and noise cancellation

Application for adaptive filtering, i.e. attenuation of undesired echo in a telecommunication network, provided by modelling the echo path using an adaptive filter and subtracting the echo path output approximation, [54].

### o Digital mobile telephony

Digital signal processors embedded in mobile phones are used for signal and data processing (e.g. for speech coding, measuring consolidation of signals, voice mail, modulation and demodulation, etc.). Modern DSP chips are optimized for wireless communication, and they provide affordable and high-quality products, [55], [56].

### 0 Digital television

Interactivity, internet access, shopping, recording shows for watching later, etc. are just some examples of what digital television provides to consumers. DSP plays a key role in the processing, coding/decoding and modulation/demodulation of video and audio signals. For example, compressed video and audio before transfer and perfect image and voice are impossible without DSP, [55].

### o Digital audio adjustment of the voice

The major example of DSP application is the improvement of audio quality and its functionality. Audio adjustment of different voices is used in film, television and radio engineering to develop the sound background, [55].

o Creating artificial speech

With the development of semiconductor technology and digital signal processors, artificial voices have almost assumed the voice quality of real human speech (e.g. Speak and Spell, TI, 1982.), [55].

### o Speech recognition

The speech recognition system is based on a training system for the recognition, digitization, and storage of every spoken word. The recognition step is based on the search for matching words for every spoken word which is digitized and saved in the base. The problem occurs when the system cannot recognize speech, e.g. due to the insufficient breaks between words, fast speaking, unclear word pronunciation or presence of background noises. To resolve these problems, DSP has two major operations: parameter insulation (in order to create a sample, a clean pattern is chosen from spoken word) and pattern matching (pattern is compared with patterns in memory), [55].

Biomedical applications

Most modern medical applications, such as electrocardiography (ECG), digital stethoscopes, pulse oximeters, etc., require DSP processing. One of the DSP processors appropriate for that application is Texas Instruments TMS320C5515, based on fixed-point arithmetic. Texas Instruments has developed an MDK (Medical Development Kit) based on the C5515 DSP processor that supports all developing medical applications, [57].

o Electrocardiography monitoring

Electrocardiography (ECG) is a procedure for data collection about the electrophysiology of the human heart. DSP is needed to read digital signals from an analogue-to-digital converter (ADC) over a serial peripheral interface (SPI), for noise reduction and for decoupling the key features of the ECG, [55].

o Anaesthesia control

An automated closed control system with embedded DSP processor for separating signals which come from brain serves to control the anaesthetic in the patient's body and to monitor the patient's condition. DSP plays a key role in the separation of auditory evoked response (AER) from background EEG signal. AER is part of the EEG signal: a few times weaker, but a significant signal. AER is an electrical reaction of the brain to external sounds, so it is essential for a transition assessment from consciousness to unconsciousness when the patient is anaesthetized, [55]

### Meteorology

DSP is used for temperature control of the sensor wire at constant temperature used in wind speed measuring instruments. DSP executes extra operations such as linearizing the output voltage of anemometers and controlling the user interface directly or using a control program on a master computer, [58].

## 4 PRACTICAL IMPLEMENTATION OF THE EVALUATION MODEL

The TMDXEVM8148 evaluation model is based on Texas Instruments processor DM814x/AM387x for developing applications sensitive to power supply, consumer, and medical video applications which require less video streaming, [59]. The digital media processor (DM8148) provides fast and high-quality creation of unique applications such as video security, video conferencing, navigation, advanced portable consumer electronic devices with high end gaming support, digital signage, smart home controller applications, etc. The evaluation model has two processors: master ARM Cortex-A8 processor, which goes up to 1 GHz, and slave processor TI C674x VLIW DSP which goes up to 750 MHz, [59], [60].

EVM works with GStreamer, which helps in creating programs for parallel execution and creates different multimedia applications: streaming, video editing, etc. The C6Accel API allows the memory share between DSP and ARM, i.e. parallel working. Generally, it is used for easy intercommunication between the ARM and DSP. The C674x processor architecture contains a bi-level internal core, the cache memory with the support of external memory. On the first level, the memory is divided into L1P (software cache) and the L1D (data cache). If the requested information is not contained in the cache memory, it is then retrieved from the next lower program levels: L2 or external memory, [10]. The architecture of the cache processor C674x is shown in Fig. 4. L1PChronic and L1D are built into the SRAM cache to 32 KB. All memory and data paths are controlled by the cache memory controller, [61].



Figure 4: Architecture of the cache processor C674x

The registers ensure the control setting mode and control various processor operations. Interrupt Controller (INTC) is responsible for the control of the interruption in the program and management of the CPU. More details about execution time comparison can be found in, [62].

Let us consider a numerical example. An executing program is given for the Monte Carlo method used in numerical integration functions executed in an integrated development environment (IDE) of the Code Composer Studio (CCSv5) supported by Texas Instruments microcontroller and embedded processors. Execution time of the loop on the digital signal processor without the level of optimization is  $3.1373 \times 10^{-206}$  seconds.

If the optimization level is set, the execution time of the loop of the numerical integration with the Monte Carlo method is  $1.112554 \times 10^{-300}$  seconds. For comparison, the execution time of the loop of the numerical integration with the Monte Carlo method on AMD Dual-Core 2.30 GHz processor is 8.78 seconds.

The main problem for an image-and-video processing system is the time of algorithm execution. Different methods for minimization operations and memory access use a different algorithm in every loop iteration, and most of the methods for execution time minimization are based on a pipeline.

Results and execution time comparisons of the image processing from a camera in different stages are presented in Table 3. It can be concluded that the digital signal processor is a better choice for image processing in comparison with other processors regarding the execution time. More examples of execution time comparisons can be found in [63].

Function	Matlab (ms)	ARM (ms)	DSP (ms)
Transform	1536	35.41	36.2
Gaussian filter	252	5.8	3.1
Horizontal interpolation	621.20	6.9	4.7
DX filter	920.3	5.4	0.2

Table 3: Execution time for various functions using different processors

# 5 DISCUSSION

Due to increasing demand for better performance of processing, there are possibilities for improving performance in clock rate, data and instruction level parallelism, decreasing the switching time of the device, etc., [64]. Owing to the demand for different multiple applications and the possibilities of running multiple tasks, high-performance processors have been developed. Classification of the microprocessors is presented in Figure 5.



Figure 5: Classification of microprocessors

General purpose processors (GPP) are used in CPUs for PCs and workstations, and have a general purpose. DSPs are microprocessors specialized for signal processing applications and embedded in mobile devices in order to optimise performance and energy consumption, [65]. Nowadays, multi-core processors in PCs use parallel running instructions, and are based on shared or distributed cache memory and can execute up to four instructions per cycle, while high-performance DSP can execute up to eight instructions per cycle, [66]. GPPs generally have Single Instruction Multiple Data (SIMD) architecture to improve their performance in data processing, [67], while DSP has very long instruction word (VLIW) or SIMD operations to improve their performance, as mentioned above.

## 6 CONCLUSION

Digital signal processors have been undergoing massive development in the last ten years, and they are embedded in different devices (from cell phones to advanced scientific devices).

The particularity of the DSP architecture enables the development of fast and efficient applications in all areas of human activity. Due to the basic architecture of the processor regarding the data collection, data processing and transmission, the DSP achieves its maximum in millions of instructions per second. Although developers of the GPP have increased its performance, the GPP with SIMD has the ability to compute intermediate complex instructions only. Furthermore, GPP includes DSP instructions and implements DSP algorithms but it still often provides only partial solutions, [67], [68].

Practical results, as described in Section 4, show the great advantages of the DSP in comparison with commonly used processors regarding the execution time of the numerical integration.

This paper gives a review of the basic architecture of DSP and the diversity of its application. Digital signal processors may be of great interest to developers who work on application development in these, or similar areas.

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# DIMENSIONAL ACCURACY OF PROTOTYPES MADE WITH FDM TECHNOLOGY

# DIMENZIJSKA NATANČNOST PROTOTIPOV PROIZVEDENIH S FDM TEHNOLOGIJO

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Keywords: additive technology, 3D printing, 3D scanning, fused deposition modelling

# Abstract

Under the term "additive manufacturing", commonly known as 3D printing, we distinguish various methods of manufacturing technologies. Common to all these processes is manufacturing a model layer by layer from a digital form. The aim of this paper is to experimentally determine which material provides dimensionally more accurate prototypes on a Fused Deposition Modelling (FDM) additive machine. Acrylonitrile Butadiene Styrene (ABS) and PolyLactic Acid (PLA) materials were used. The dimensional accuracy was checked by comparing the Computer-Aided Design (CAD) model with each of ten models obtained by the method of 3D scanning. The results show that prototypes manufactured from PLA are dimensionally more accurate those made from ABS.

## **Povzetek**

Pod izrazom proizvodnja z dodajanjem materiala oziroma pogosteje uporabljenim izrazom 3D tiskanje ločimo različne metode proizvodnih tehnologij. Skupno vsem procesom je proizvodnja modela po plast za plastjo iz digitalne oblike. Namen tega prispevka je eksperimentalno določiti, kateri material zagotavlja dimenzijsko natančnejše prototipe izdelane s FDM tiskalnikom. Uporabljena sta bila 2 materiala akrilonitrilbutadienstiren (ABS) in polimlečna kislina (PLA).

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Dimenzijska natančnost je bila preverjena tako, da je bilo vseh deset natisnjenih modelov pretvorjenih v računalniške s pomočjo skeniranja in nato primerjani z modeliranim računalniškim modelom. Rezultati kažejo, da so prototipi izdelani iz PLA materiala dimenzijsko natančnejši od prototipov izdelanih iz ABS materiala.

## 1 INTRODUCTION

Fused Deposition Modelling (FDM) is an additive manufacturing process by which a model, prototype or finished product is manufactured. The process was invented by Crump in the late 1980s, and the procedure has been commercially available since 1990. It is also known as FFF (fused filament fabrication) process or PJP (plastic jet printing). Upon the expiration of the patent for this technology, the possibility of creating affordable 3D printers for homes and offices has emerged. Equipment that cost \$20,000 in 2010 now costs less than \$1,000, [1]. Although the technology has become widely accepted it has some limitations, such as layer thickness, and producing very thin walls that are prone to warping, etc., [2].

For this work, the FlashForge Creator X device with two nozzles (two extruder heads) was used. The device has relatively small dimensions and can be used as office equipment (Figure 1).



Figure 1: FDM machine Flashforge Creator X.

As with all other FDM devices, the material is supplied to the head with a plastic (teflon) tube guide. The material is in the form of a wire with a diameter of 1.75 mm wound on a drum located on the rear panel. The principle of operation is as with other FDM devices. The workpiece is created layer by layer in the direction of the z-axis. The extruder head with the nozzles is shifted in the x- and y-axes using an electric motor, belt, and metal rails. After applying the first layer, the work bed is lowered to a height of one layer in the z-axis, and the next layer is printed. The procedure is repeated until the last layer is finished.

Currently a wide variety of materials is available, but the most commonly used are Acrylonitrile Butadiene Styrene (ABS) and PolyLactic Acid (PLA), [3].

Some studies report the dimensional properties of different materials used in FDM technology, but they mostly depend on orientation, layer thickness, machine, curing, etc., [4-6].

## 2 DESIGN

The first step in our experiment was modelling the body of the electronic casing (3D model) in SolidWorks 2014 (Figure 2). A wall thickness of only 2 mm is a major problem when manufacturing on a desktop FDM device. Prototypes with thin and high walls (requiring a long time to manufacture) made on this device are not as dimensionally stable as prototypes made on industrial devices. In practice, the device had problems with both materials. ABS had a greater tendency to warping visually or splitting away from the work bench. With using PLA material, there were difficulties in clogging of the extruder.

Strains occur due to differences in temperature between the work bed and the workpiece, and that also includes the temperature difference between the separate layers of the workpiece along the z-axis, [2]. The tendency of the material to warp may also depend on its chemical composition.

Separation of the two layers while printing is called "stratification", which is a relatively frequent phenomenon when printing with ABS material. Stratification is eliminated by installing the device in a place with no draft, which rapidly cools the workpiece. Newer generations of FDM devices have acrylic panels for outer protection.



Figure 2: 3D model of electronic casing.

## 3 MANUFACTURING ON FDM MACHINE

After designing the virtual product or 3D model, the next step is converting it to STL (Standard Tessellation Language) file format and manufacturing it with the FDM device. Ten prototypes were printed: five in ABS (white casing), and five in PLA material (blue casing). The casing has dimensions of  $100 \times 60 \times 41$  mm (L×W×H) with a wall thickness of 2 mm.

When printing ABS material, the following parameters were used (Table 1). Infill of only 10% was used in order to save on material and reduce printing time. This type of device is not suitable for working with the infill from 70–100%, because the results are poor in appearance and quality. A layer height of 0.20 mm is the standard option for this device. The working temperature of the heated workbed is usually set between 100 and 110 °C (Table 1).

SETTINGS	ABS	PLA
Infill (%)	10	10
Layer thickness, mm	0.2	0.2
Extruder temperature, (°C)	225	210
Work bed temperature, (°C)	102	60
Extrusion speed while printing, (mm/s)	60	60
Extrusion speed while changing position, (mm/s)	90	90

**Table 1:** Settings used while printing in ABS and PLA material.

While printing PLA material, some settings needed to be changed. Layer height and extrusion speed remained identical. The temperature of the heated work bed was changed and set to 60 °C. The temperature of the extruder was set to 210 °C (Table 1). All ten prototypes were made over a time interval of ten days in closed office space so that external influences were minimal (Figure 3).



Figure 3: Finished prototype in PLA material.

## 4 3D SCANNING

The process of digitalization was done on a Steinbichler Optotechnik series Comet5 1.4M industrial 3D scanner. The process of digitizing (3D scanning) with this equipment is very quick, easy, and accurate. The characteristics of the device are listed in Table 2.

Measuring volume (x,y,z)	46×34×50 mm <sup>3</sup>	
Camera resolution	1.4 Mpx	
Measuring distance (z)	850 mm	
Measuring distance of neighbour points	0.033 mm	
(x,y)	0.000 mm	
Capturing time	2 sec. (high-speed module)	
Light source	200 W	
Supported data formats	CATIA V4/V5, IGES, STEP, Pro/E, TXT, STL	

Table 2: Characteristics of 3D scanner.

Prototypes made from PLA had highly reflective surfaces, which are difficult to digitize so they were sprayed with a very thin layer of non-reflective white coating. White products from ABS had matte surfaces and did not have this problem.

The aim of digitization is to obtain an STL file or a 3D model of the manufactured prototype on the computer. A product that is digitized is positioned on a rotating table. The computer program operating the scanner was adjusted to the desired number of images to digitize over a full rotation (360°) of the stand. If the number of desired images is set to 10, for example, the table is rotated by 36° for each picture. After a full circle, the computer screen displays a 3D model of a digitized product. It is necessary to review the model to detect potential flaws or errors. Sometimes it is necessary to fill holes on the surface of the model, because it was not well digitized, or to repeat scans at certain custom angles. These are common phenomena during this procedure. Constant temperature and light are conditions in which digitization should be conducted. The 3D scanner comprises a temperature sensor reads a temperature above or below the set limits, the device disables recording. The amount of light should be constant (best with no light), because it directly affects the digitizing, or appearance of the 3D model. To prevent light affecting accuracy, measurements were taken in a dark room isolated from outer environmental light.

## 5 RESULTS

Comparison of dimensions between CAD and digitized 3D model is possible by using a computer program to check deviations. INSPECTplus software allows users to align scan data with other scan data or CAD 3D models. Once aligned, the user can generate surface comparison reports, comparisons of cross sections and border lines with needle diagrams, feature comparisons and traditional measurements. Select the CAD model (ideal computer model), in this case called "box ver 8". Next, select the model prepared by the process of digitalization. Products in this

paper are marked as ABS and PLA 1-5 to prevent confusion during the processing of results. Furthermore, to compare the dimensions, it is necessary to align the models in the same coordinate system. To align the models, the best fit option is selected (Figure 4).

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Figure 4: Alignment of CAD (blue) and digitized model (grey).

The next step is to check the values of deviation. The easiest way to achieve this is by the inclusion of the so-called "Color table" representation that uses different colours to mark deviations in the model being checked. Red defines deviations in the positive direction (surfaces placed or leaning outside the CAD model) and blue in the negative direction (surfaces placed to the interior of the CAD model). Maximum deviation limits on the "Color table" (dark red and dark blue) can be set by the user, and are often selected by trial and error until a satisfactory representation is generated.

Finally, it is possible to analyse deviations for any selected point on the model using the "Flyer" tool. For the purpose of this paper, the point of maximum deviation in the positive and negative direction was read for every digitized model (Figure 5).



Figure 5: Deviation of dimensions on prototype "ABS 2".

Prior to the analysis of results, the readings had to be systematized. Accordingly, every surface on the model was marked with a cipher so they could be correlated with certain areas (surfaces/faces) on the model when determining the deviations (Figure 6).



Figure 6: Faces of the model with markings.

Analysing the results in Table 3, clearly there are minor deviations in the production of the PLA material prototypes. Product ABS 3 has the largest recorded deviation of 1.01 mm. The reason for such a deviation in geometry is probably an error in material while manufacturing. More specifically, it is possible that some impurities appeared in the material and affected the final result.

Observing the locations of the maximum deviations in the negative direction (indentation of material) for both PLA and ABS, we can see constant repetition of the front (50%) and back faces (50%). Since these sides are the longest, they tend to have the largest indentations because there was no reinforcement on those sides. When the top layers are printed, the material cools, contracts and pulls the sides closer. To eliminate these deformations, some reinforcements should be added in the form of ribs to provide more strength to the faces

(FF/BF). In 70% of the cases, maximum deviations in the positive direction are located either on the left (LF) or right faces (RF) due to the warping of the material. While printing, the edges (LF/RF) first start to pull away from the work bed so that probably caused the deviations. In 30% of the cases, the maximum deviation occurred on the top face, probably due to impurities in the material.

When compared, prototypes made from PLA showed fewer deformations and were more stable and warp-resilient. Table 3 summarizes all the data collected.

PROTOTYPE	MAX. POSITIVE DEVIATION (mm)	FACE	MAX. NEGATIVE DEVIATION (mm)	FACE
ABS 1	0.70	RF	- 0.75	FF
ABS 2	0.73	RF	- 0.82	FF
ABS 3	1.01	TF	- 0.67	BF
ABS 4	0.79	TF	- 0.73	FF
ABS 5	0.70	RF	- 0.70	FF
ABS <sub>AVG</sub>	0.79 ± 0.13		- 0.73 ± 0.06	
PLA 1	0.26	RF	- 0.59	BF
PLA 2	0.24	TF	- 0.52	BF
PLA 3	0.26	RF	- 0.54	BF
PLA 4	0.24	LF	- 0.53	BF
PLA 5	0.39	LF	- 0.52	FF
PLA <sub>AVG</sub>	0.28 ± 0.06		- 0.54 ± 0.03	

Table 3: Measured results.

Total average deviation of ABS is  $0.79 \pm 0.13$  and  $-0.734 \pm 0.06$ . The deviation of PLA prototypes is  $0.28 \pm 0.06$  and  $-0.54 \pm 0.03$ . This means that prototypes from PLA were more accurate and dimensionally stable than those made from ABS.

## 6 CONCLUSION

The aim of this study was to experimentally investigate which material produces more dimensionally accurate prototypes. ABS and PLA materials, which are commonly used with FDM technology, were tested. The dimensional accuracy check was performed by comparing the CAD model with each of the ten digitized prototypes. Comparing the results of maximum deviations leads to the conclusion that the manufacturing of products with thin walls while using PLA material leads to smaller deviations in geometry.

In this case analysis, but accompanied by general experience, has shown that regardless of the geometry of the prototype, they are more accurate when manufactured from PLA material.

In office environments, it is safe to leave the device in operation, while working on another project. ABS generally requires more attention while printing to detect errors in a timely manner.

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# DETERMINING THE CURRENT CAPACITY OF TRANSMISSION LINES BASED ON AMBIENT CONDITIONS

# DOLOČANJE TRENUTNE ZMOGLJIVOSTI DALJNOVODOV NA OSNOVI ZUNANJIH POGOJEV

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**Keywords:** powerline ampacity system, conductor capacity, overhead lines, ambient conditions, ACSR rope 350/59

# Abstract

After the incorrect prediction of generation from renewable sources, overloading of transmission lines occurred, resulting in the need for subsequent construction of new transmission lines and the maximum exploitation of existing power lines. One means of achieving this is to determine the permissible current load of power lines while respecting the surrounding climatic conditions. This article deals with determining the maximum current load of the power lines for changing various surrounding factors. The calculation is performed for conductor ACSR 350/59, which is used in the transmission system in Slovakia.

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## <u>Povzetek</u>

Pri povezovanju energetskih sistemov in nepravilnih predvidevanjih proizvodnje iz obnovljivih virov, je prišlo do preobremenitve daljnovodov. Tako se pojavi potreba po gradnji novih daljnovodov in čim boljši izkoriščenosti obstoječih. Eden od načinov je, da se določi dovoljena trenutna obremenitev daljnovodov ob upoštevanju okoliških vremenskih razmer. Prispevek obravnava določanje največje trenutne obremenitve daljnovoda ob različnih vremenskih dejavnikih. Izračun smo opravili za vodnik ACSR 350/59, ki se uporablja v prenosnem omrežju na Slovaškem.

## **1** INTRODUCTION

Capacity is defined as the maximum allowable value of current that can flow through transmission lines without adversely affecting the mechanical and electrical properties of the conductor. The size of the maximum permissible current value is determined by the mechanical and electrical properties, its ability to dissipate the heat generated inside the conductor, and the ambient conditions, [1].

The necessity of raising the capacity of transmission lines has begun to emerge in recent years after a massive deployment of renewable energy sources (due to lack of line capacity on north-south routes within a UCTE grouping), which overloaded the lines due to the insufficient prediction of the generation of electricity from renewable sources, [2].

For these reasons, the construction of new transmission lines is necessary, which represents a considerable financial and time-consuming solution. One alternative is to focus on determining the maximum permissible currents depending on ambient environmental conditions, which may serve the supervisory control of power flows on uncongested lines.

## 2 THEORETICAL INTRODUCTION TO THE CAPACITY OF THE TRANSMISSION LINES

As mentioned previously, the concept of capacity means the maximum permissible value of current that can flow without disturbing the conductor's electrical and mechanical properties. Capacity size depends on the electrical and mechanical properties of the conductor, its ability to spread the heat generated, and the ambient conditions, [3].

Ambient conditions are all climatic environment in which the line is placed. Among the climatic conditions are ambient temperature, speed and direction of wind flow, intensity of solar radiation, and precipitation, [3].

The most commonly used types of conductors in our transmission system include ACSR ropes, which, depending on the voltage levels, are arranged individually or in bundles. For the purposes of this article, the effects of environmental conditions on the size of the maximum permissible value of the current ACSR 350/59 rope will be discussed.

The parameters of the rope are shown in the table below (Table 1).

Rope Туре	ACSR 350/59
Rope diameter (mm)	26.39
Rope cross-section (mm <sup>2</sup> )	410.80
Nominal weight (kg.km <sup>-1</sup> )	1453.01
Specific gravity (MN.m <sup>-3</sup> )	0.03469
The maximum permissible stresses (MPa)	108.661
Elastic modulus (MPa)	74332
The coefficient of thermal expansion (1/°C) .10 <sup>-6</sup>	18.65
Rated DC resistance (Ω/km)	0.0835

Table 1: Parameters of the rope, [4]

For the construction of power lines in the currently applicable EN 50341 standard, the maximum temperature of the conductor is 70  $^{\circ}$ C.

The actual control of temperature of the conductor in the case of known current value is performed for the following conditions:

- The current load is the highest,
- Ambient temperature is 35 °C,
- Wind speed is 0.5 m/s at a 45 ° angle of impact,
- Global temperature of sunlight is 1000 W/m<sup>2</sup>,
- Absorption coefficient is 0.5,
- Emissivity coefficient of 0.5, [5].

Under these conditions, it can be said that the lines are designed for the worst possible environmental conditions so as not to exceed the maximum permissible conductor temperature. It should be noted that the above climatic conditions rarely occur, resulting in a certain margin for the maximum permissible value of the current that is not in constantly changing environmental conditions can be achieved, and thus the line can be overloaded.

## 3 DETERMINATION OF MAXIMUM ALLOWABLE CURRENT VALUE

The dependence of the size of permissible currents for the electrical and mechanical properties of the conductor can be, provided that there is no damage to the effects of heat, considered as constant, given at the factory.

The evaluation of environmental conditions, as factors that determine the maximum permissible load of the conductor, must be based on their variability over time.

The steady state temperature of the driver, when considering the environmental conditions can be expressed by the following equation (3.1), where left part of the equation form variables involved in increasing the temperature of the conductor, and a right part of the equation form parameters involved in the cooling section, [6].

$$P_Z + P_S + P_C = C_v \cdot \frac{d\Theta}{dt} + P_k + P_r + P_w$$
(3.1)

In calculation, conductor warming due to the corona is neglected. The most significant increase in temperature due to the corona occurs mostly during clashes when the cooling of the conductor is highest, and thus we neglect the contribution cooling of the conductor due to the water evaporation, [6].

For the purposes of this publication, we will base the solution from aforementioned formula of the static model, which does not change the load, the change in temperature of conductor; thus, balance equation (3.1) will have the following form (3.2), [6].

$$P_Z + P_S = P_k + P_r \tag{3.2}$$

Determining the impact of individual surrounding factors to the resulting current capacity of conductor will be based on the initial conditions defined by the EN 50341 standards:

- We will examine the contribution of solar radiation by changing the intensity of it in the range of 100 W/m<sup>2</sup>-1000 W/m<sup>2</sup> under constant environmental conditions given by the standard, provided the maximum recommended temperature of the ACSR rope 350/59 does not to exceed 70 °C,
- We will examine contribution of the ambient temperature in the range -40 °C to -1 °C and in the range of + 1 °C to 40 °C under constant environmental conditions given by the standard, provided the maximum recommended temperature of the ACSR rope 350/59 does not to exceed 70 °C,
- 3. We will examine contribution of wind speed in the range of 1 m/s to 40 m / s under constant environmental conditions given by the standard, provided the maximum recommended temperature of the ACSR rope 350/59 does not to exceed 70 °C.

### 3.1 Impact of solar radiation on the maximum permissible current value

Solar radiation that irradiates the examined conductor has three components: direct radiation, diffuse radiation and reflected radiation, [6].

In determining thermal growth with sufficient accuracy, the diffuse and reflected light, whose effect is 2-4%, can be excluded, [6].

Dependence of the maximum permissible value of the current on the size of the intensity of solar radiation is shown in the figure below (Figure 1).



*Figure 1:* Dependence of the maximum permissible value of the current on the intensity of solar radiation

As is clear from the previous figure, change of the intensity of solar radiation leads to linear change of the maximum permissible current value. In the investigated interval of solar irradiation (100W/m<sup>2</sup> to 1000W/m<sup>2</sup>), the maximum permissible value for the current interval 790.07 A was reached at the lowest intensity of solar radiation and at a maximum intensity of solar radiation 711.22 A for a one-in-three wire bundle. The above allowed current capacity of the conductor with a minimum intensity of solar radiation is an increase in the capacity of the line to the state with the maximum intensity of solar radiation by 11%.

### 3.2 Impact of air flow on the maximum allowed value of current

Airflow from the perspective of reducing the temperature of conductor represents a transfer of energy in macroscopic scale, between the particles of the body containing a large number of molecules. This process is dependent on the character of hydrodynamic and thermal marginal layer; the shape and size are affected by the speed and direction of air flow, [6].

When examining the impact of air flow, the change of the maximum permissible currents at different wind speeds at an interval of 1 m/s to 40 m/s at an angle of impact to the power line 45° will be monitored.

The dependence of the maximum permissible current value when changing the air velocity is shown in the figure below (Figure 2).



Figure 2: Dependence of the maximum permissible value of the current on air velocity

From the figure, we can see that with increasing air speed leads to exponential increase of the maximum permissible current value. The most significant increase in the maximum current value occurs in the interval velocity of 1 m/s to 15 m/s, with an increase in the allowable load of 711.22A to 1567.55A, representing an increase of 120% of the initial value.

In the examined range of action, the wind flow velocity to the maximum permissible current value from 15 m/s to 40 m/s occurs near a linear increase of the maximum permissible value current from 1567.55A to the 2099.70A.

### 3.3 Impact of radiation to the maximum permissible value of the current

The radiation represents a mechanism of heat transfer, which consists of the emission and absorption of the electromagnetic radiation. An object with a non-zero temperature emits electromagnetic radiation, according to Planck's law, [6] [7].

The total amount of energy emitted from the surface of the object increases with surface temperature. Depending on the temperature of the body surface, the emission spectrum changes. With the increase of the temperature, there is a change of the spectrum to shorter wavelengths. In addition to its own radiation, each object captures the photons radiated by nearby objects. The resulting energy balance of the process is given by the difference of radiated and received energy. As the amount of radiated energy increases with temperature, the resulting radiation is the transfer of energy from warmer units to cooler ones, [6] [7].

Studying the effect of radiation on the final current capacity will be based on the assumption that the conductor temperature is constant at 70 ° C. The examination will include the impact of ambient temperature on the maximum permissible current load at an operating temperature of 70 °C. The interval examination will consist of two parts, in the first range of -40 °C to 1 °C; in the second part, we will examine the influence of the positive ambient temperature in the scope of 1 °C to 40 °C.

Dependence of the maximum permissible current value when ambient temperature changes for the first and second studied interval are in the following figures (Figure 3, Figure 4).



Figure 3: Dependence of the maximum permissible value of current on ambient temperature of the first examined interval



*Figure 4:* Dependence of the maximum permissible value of current on ambient temperature of the second examined interval

From the figures above, we can see that with increasing ambient temperature leads to decrease of the maximum permissible current value. This change ampacity occurs as a direct result of changes in the coefficient of heat loss by radiation ( $P_r$ ), wherein in increasing the ambient temperature leads to inversely proportional heat rejection to the environment.

In terms of size ampacity in the first interval, there is a decrease in the permissible current value from 1330.23 A to 1061.63 A. For the second period, there was a decrease in the permitted current value from 1045.63 A to 645.74 A. For the first interval, the decrease was nearly 20.19%, but in the second interval at positive ambient temperature, this change is more pronounced. For the second interval, there was a decrease the maximum permissible current value for the conductor ACSR 350/59 by 38.24%.

## 4 CONCLUSION

Determining permissible current load in real time is an important and highly relevant issue in professional circles. In recent years, what is needed is to increase the capacity of transmission systems. The first option is the construction of new lines; however, this is a time-consuming and costly solution. The second option is to maximize the use of existing transmission lines in knowledge of environmental conditions and taking into account their impact on the maximum permissible current load in terms of the standard recommended temperature.

This article describes the different environmental factors affecting the maximum permissible current load at a maximum conductor temperature of 70 °C and examines their impact on the final ampacity of lines. The resulting current load has been studied for an electrical conductor in the three-volume configuration of one phase for the voltage level 400 kV.

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### Nomenclature

- Pz conductor warming influence current flow
- *Ps* conductor warming influence of sunlight
- Pc conductor warming influence the corona
- **C**<sub>V</sub> heat capacity of conductor
- **P**<sub>K</sub> conductor cooling influence air flow
- **P**<sub>R</sub> conductor cooling influence radiation
- **P**<sub>W</sub> conductor cooling influence water evaporation





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# MAIN TITLE OF THE PAPER SLOVENIAN TITLE

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## **Povzetek**

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### (Arial bold, 10pt, after paragraph 6pt space)

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Equation

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*Figure 1:* Name of the figure (centred, on bottom of figure, photo, or drawing)

## References

- [1] N. Surname: *Title,* Journal Title, Vol., Iss., p.p., Year of Publication
- [2] N. Surname: *Title,* Publisher, Year of Publication
- [3] **N. Surname:** *Title* [online], Publisher or Journal Title, Vol., Iss., p.p., Year of Publication. Available: website (date accessed)

## Examples:

- [1] J. Usenik: Mathematical model of the power supply system control, Journal of Energy Technology, Vol. 2, Iss. 3, p.p. 29 46, 2009
- [2] J. J. DiStefano, A.R. Stubberud, I. J. Williams: Theory and Problems of Feedback and Control Systems, McGraw-Hill Book Company, 1987
- T. Žagar, L. Kegel: Preparation of National programme for SF and RW management taking into account the possible future evolution of ERDO [online], Journal of Energy Technology, Vol. 9, Iss. 1, p.p. 39 50, 2016. Available: <u>http://www.fe.um.si/images/jet /Volume 9 Issue1/03-JET marec 2016-PREPARATION OF NATIONAL.pdf</u> (7. 10. 2016)

Example of reference-1 citation: In text [1], text continue.

## Nomenclature

(Symbols) (Symbol meaning)

t time





TSSN

